

Teorema. f differenziabile in $x_0 \iff f$ derivabile in x_0 . In tal caso $\lambda = f'(x_0)$.

Dim. $f(x) = f(x_0) + \lambda(x - x_0) + o(x - x_0)$ per $x \rightarrow x_0$

$$\iff \lim_{x \rightarrow x_0} \frac{f(x) - f(x_0) - \lambda(x - x_0)}{x - x_0} = 0 \iff$$

$$\lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0} = \lambda.$$

□

f derivabile in x_0

$$\Rightarrow \underbrace{f(x) - \left(f(x_0) + f'(x_0)(x - x_0) \right)}_{\text{green bracket}} = o(x - x_0), x \rightarrow x_0$$

